

Delocalised Niagara Falls in the Financial Industry

XXXV Heidelberg Physics Graduate Days

Heidelberg, October 7th, 2015

Agenda

- » The Basics: Cash flow valuation and credit risk modeling
- » From the basics of bond valuation to securitizations: correlation and waterfalls
- » Real world example

The Basics: Cash flow valuation and credit risk modeling

Vocabulary & Concepts: Mark to Market and Mark to Model (1/2)

- » Primary market
 - > When securities are first issued
 - > Fixed income securities are usually structured so that their issue price is equal to par, e.g. nominal EUR 1000, coupon 3,25%, issue price $P(t_0) = EUR \ 1000$
- » Secondary market
 - > Market for securities that have already been issued and are now being traded
 - > Prices can deviate significantly from the issue price



When talking about the price of a security, one usually refers to its price in the secondary market.

*Yield ≠ Coupon

Vocabulary & Concepts: Mark to Market and Mark to Model (2/2)

- Prices of liquid securities like common shares and "plain vanilla" bonds of large corporations can be observed directly in the market => mark to market
- » Securities can be illiquid for a variety of reasons
 - > Supply and demand: few suitable investors, lack of market makers
 - > High risk; "distressed" securities
 - > Difficulty to assign a value
- Mark to model determine the current 'hypothetical' market value for illiquid instruments; For this a pricing model must to be used. This needs to be done for:
 - > accounting purposes
 - > Monitoring / risk management
 - > when up for sale
- » Securitizations usually do not have a liquid secondary market

Price of securitizations needs to be calculated often by a model.

Vocabulary & Concepts: Typical Cash Flow Series for Debt

Bullet repayment (e.g. fixed rate bond)



Zero repayment (e.g. zero bond)

Annuity repayment (e.g. mortgage)



Linear repayment



Vocabulary & Concepts: Time Value of Money & Present Value (Short Recap)

» What is better: Receive EUR 100 today OR receive EUR 100 in one year?

| | T=0 | Invest at the risk fro rate, e.g. 3% | ee T=1 |
|------------|---------|---|---------|
| Scenario 1 | EUR 100 | | EUR 103 |
| Scenario 2 | | | EUR 100 |

- » Time value of money The value of a cash flow depends on the time at which it occurs
- » Present value:
 - > Current value of future series of cash flows

| | T=1 | T=2 | T=3 | Present Value |
|-------------|---------|---------|---------|--|
| CF Series 1 | EUR 100 | EUR 100 | EUR 100 | $PV = \frac{100}{(1,03)^1} + \frac{100}{(1,03)^2} + \frac{100}{(1,03)^3} = 282,86$ |
| CF Series 2 | EUR 0 | EUR 0 | EUR 305 | $PV = \frac{305}{(1,03)^3} = 279,12$ |

The present value is a method to make different cash flow series comparable.

Vocabulary & Concepts: Present Value

» More formally, the present value of a series of cash flows is calculated by summing up the discounted cash flows:

$$PV = \sum_{i}^{n} CF^{i} \cdot D(t_{i})$$

- » D(t) is the so called *discount factor* and is defined as today's value of a risk adjusted payment of one monetary unit at a future time $t \ge 0$.
- D(t) is calculated depending on how many times per year interest is paid (assuming reinvestment of interest payments)
 - > Annual compounding: $D(t) = (1 + r)^{-t}$
 - > *m* times compounding: $D(t) = \left(1 + \frac{r}{m}\right)^{-mt}$
 - > Continuous compounding: $D(t) = \lim_{m \to \infty} \left(1 + \frac{r}{m}\right)^{-mt} = e^{-rt}$ (most common assumption)

The present value is an essential tool for valuing financial instruments.

- » Consider the following (hypothetical) example:
 - > Riskless bond: coupon c = 3% (paid annually), maturity 3 years, nominal EUR 100
 - > Risk free rate: r = 3%

$$P(t_0) = PV = \sum_{i=1}^{n} CF^i \cdot D(t_i) = \frac{3}{(1+r)^1} + \frac{3}{(1+r)^2} + \frac{103}{(1+r)^3} = EUR \ 100 \ (= N \ or \ "par")$$

- > Risky (corporate) bond: coupon c = 5%, maturity 3 years, nominal EUR 100
- > Issue price $P(t_0) = \text{EUR } 100$, however $PV = EUR \ 105,66$
- > This implies an expected loss of EUR 5,66 over the life of the bond! Moreover from this can be deducted that the "correct" rate for discounting the **contractual** cashflows is not r = 3%, but $\hat{r} = 5\%$.
- > The difference of 2% is the compensation for bearing the risk of the corporate bond

Valuation of fixed income securities in general is built on quantifying risk and return of these securities.

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Vocabulary & Concepts: Modeling Cash Flows and Credit Risk (2/2)

Normally, cash flows are risky, so 'present value' is understood to be the present value of a series of *expected* cash flows: $\sum_{n=1}^{n}$

$$PV = \sum_{i} CF_{exp}^{i} \cdot D(t_{i})$$

- » For fixed income:
 - > modeling cash flows $\leftarrow \rightarrow$ modeling credit risk (or default risk) over time
 - Cash flows = scheduled payments expected losses
- » Basic Equation for Expected Loss: $E(L) = E(EAD) \cdot E(LGD) \cdot PD$

EAD: Exposure at defaultLGD: Loss given defaultPD: Probability of default

Credit risk models can be calibrated using different kind of data:

- CDS (Credit Default Swap) spread curves
- CDS-sector curves as proxies
- historical default rates based on e.g. ratings/sectors

- + reflects view of investors + forward looking
- + Alternative if no market data available

Vocabulary & Concepts: A simple Model for Credit Risk (1/2)

| PD(t): Cumulative probability of default | Probability of there having been any default up to a particular point in time |
|--|---|
| PS(t): Cumulative probability of survival | Probability of there having been no default up to a particular point in time |
| $PD(t_1, t_2)$: Unconditional probability of default | Probability of there being a default between t_1 and t_2 $(t_1 < t_2)$ as seen from today |
| $PD_{cond}(t_1, t_2)$: Conditional probability of default (or hazard rate λ for small time intervals) | Probability of there being a default in a given period, conditional on there not having been a default up to that period. |

$$PD_{cond}(t_1, t_2) = PD(t_1, t_2)/PS(t_1)$$
$$\lambda(t)\Delta t = PD(t, t + \Delta t)/PS(t) = [PS(t) - PS(t + \Delta t)]/PS(t)$$
$$PS(t + \Delta t) - PS(t) = -\lambda(t)PS(t)\Delta t$$
$$\frac{dPS(t)}{dt} = -\lambda(t)PS(t)$$
$$PS(t) = e^{-\int_0^t \lambda(\tau)d\tau} \quad (\Leftrightarrow PD(t) = 1 - e^{-\int_0^t \lambda(\tau)d\tau})$$

Taking Limits:

Solution:

Example: Moody's Rating class B has historical cumulative default rates:

| Term (years) | 1 | 2 | 3 | 4 | 5 |
|--------------|------|-------|-------|-------|-------|
| PD cum. (%) | 5,21 | 12,19 | 17,24 | 21,95 | 26,29 |

Find hazard rates using **bootstrapping** method:

»
$$PD_{cond}(0,1) = 1 - e^{-\lambda_1} = 0,0521$$
 ⇔ $\lambda_1 = 0,053506$

»
$$PD(1,2) = PS(1) - PS(2) = PD(2) - PD(1) = 12,19 - 5,21 = 6,98\%$$

»
$$PD_{cond}(1,2) = PD(1,2)/PS(1) = 0,0698/(1-0,0521) = 7,36\%$$

- » $PD_{cond}(1,2) = 1 e^{-\lambda_2} = 0,0736 \iff \lambda_2 = 0,07648$
- » $PD_{cond}(2,3) = ...$

» Check:
$$PD(2) = 1 - e^{-\int_0^2 \lambda(\tau) d\tau} = 1 - e^{-(0.0535 + 0.0765)} = 12,19\%$$

Model default rates of illiquid securities with a credit risk model that is calibrated to available market or historical data.

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From the basics of bond valuation to securitizations

Correlation and Waterfalls

From Plain Vanilla Bonds to Securitizations

- » With this understanding of default risk, we can value a simple cash flow series from a bond
- » What else is needed for the valuation of securitization:
 - » Mechanism for loss distribution between the individual tranches
 - » Understanding of correlation



Securitizations add two layers of complexity compared to plain vanilla bonds: correlation and waterfalls

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The Influence of Correlation (1/3)

- ▶ 1 Factor Merton: $Y_i(t) = \sqrt{\rho} \cdot m(t) + \sqrt{1 \rho} \cdot Z_i(t)$ describes the default process of the individual collateral pool constituents. This gaussian model is driven by
 - \rightarrow *m*(*t*): systematic factor common to all consituents
 - > $Z_i(t)$: idiosyncratic factor specific to the i_th asset
- » Semi analytical sollution gives the portfolio loss distribution



The Influence of Correlation (2/3)

» Correlation determines the shape of the portfolio loss distribution...



The Influence of Correlation (3/3)

and hence it also determines the values of the individual tranches :



» Higher correlation implies a larger likelihood of extreme events, either no losses or total loss

- > This increases the spread ("the riskiness") of the senior tranche,
- > reducing it at the same time for the first loss piece.
- » The spread curves for intermediate tranches are usually non monotonic

Investing in securitizations means having a view on asset correlations

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The Waterfall – Actual Example



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| Reference Portfolio / Underlying Loans | | | | | |
|---|---|--|--|--|--|
| Cash flow profile: Nominal Maturity Repayment style (annuity, bullet,) Prepayment assumptions Interest (fixed or floating + spread; frequency) | Credit risk: > Default rate > Recovery rate > Recovery lag | | | | |
| If no information on individual loans available loans | e, use stratification tables to derive synthetic | | | | |

General information

- > Day count convention (act/365, act/360, 30/360, ...)
- > Business day convention (following, modified following, preceding, ...)
- > Holiday calendars
- > Offsets

Modeling of the reference portfolio's cash flows will be more precise the more information is available.

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Securitization Cash Flow Model Input - A Lot of Details (2/2)

| Tranches | | | | | |
|---|---|--|--|--|--|
| Tranche details: | Tranche functionalities: | | | | |
| (Outstanding) Nominal | Treatment of lost interest | | | | |
| > Maturity | > Deferred interest | | | | |
| Coupon (frequency) | Cumulative losses | | | | |
| | Reinstatements / Revolving features | | | | |

Waterfall and Triggers

| Waterfall | Triggers based on PF performance | | | |
|---|---|--|--|--|
| Order of priority | Overcollateralization Tests | | | |
| Distribution of principal | Interest Coverage Tests | | | |
| Distribution of interest | Clean Up Trigger | | | |
| Application of losses (if applicable) | > Default Trigger | | | |
| > Pay reinstatements (if applicable) | | | | |

> IRS: maturity, reference floating rate, fixed rate, payment frequency

Elaborate cash flow engines can incorporate a broad range of contractual features to model expected cash flows as realistic as possible.

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Real World Example

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How it can be done technically

Demonstrating Excel + valuation plug-in

Case Study – FAB UK 2004-1 Ltd.

ABS CDO^2

| Key Figures | | | | | | |
|--|-------------|--|--|--|--|--|
| Format fixed & floating rate notes | | | | | | |
| Portfolio 59 mezzanine ABS CDO tranches (UK assets) | | | | | | |
| Total Notional | GBP 204,5MM | | | | | |
| Notional 31.12.2013 | GBP 141,5MM | | | | | |
| Issue Date | 6.4.2004 | | | | | |
| Maturity | 6.12.2045* | | | | | |



Complex Structure: Securitization of Securitizations → "ABS CDO^2" or "Structured Finance CDO"

* Unless redeemed before.

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FAB UK 2004-1 Ltd. – Offering Circular

OFFERING CIRCULAR FAB UK 2004-1 Limited

(incorporated in Jersey with limited liability under registered number 87004)

£157,500,000 Class A-1E Floating Rate Notes due 2045 £7,500,000 Class A-1F Zero Coupon Notes due 2045 £10,000,000 Class A-2E Floating Rate Notes due 2045 £8,800,000 Class A-3E Floating Rate Notes due 2045 £4,700,000 Class A-3F Fixed Rate Notes due 2045 £9,000,000 Class BE Floating Rate Notes due 2045 £7,000,000 Class C Subordinated Notes due 2045 £10,000,000 Class S1 Combination Notes due 2045 * £7,000,000 Class S2 Combination Notes due 2045

Issue Price - ClassA-1E Floating Rate Notes: 100 per cent., Issue Price - Class A-1F Zero Coupon Notes: 65.6608 per cent.* Issue Price - Class A-2E Floating Rate Notes: 100 per cent., Issue Price - Class A-3E Floating Rate Notes: 100 per cent., Issue Price - Class A-3F Fixed Rate Notes: 100 per cent. Issue Price - Class BE Floating Rate Notes: 100 per cent. Issue Price - Class C Subordinated Notes: 100 per cent. Issue Price - Class S1 Combination Notes: 74.2456 per cent.** Issue Price - Class S2 Combination Notes: 100 per cent.**

*The Class A-1F Notes shall bear interest from the Class A-1F Target Date (as defined below) if not fully redeemed on or prior to such date.
**Each Class S1 Combination Note consists of two "Components", a Class S1/C Component and a Class A-1F Component.
***Each Class S2 Combination Note consists of two "Components", a Class S2/C Component and a Class A-3F Component.
The initial principal amount of the Class S1 Combination Notes and the Class S2 Combination Notes above is included in the initial principal amount of the respective Components of the Class S1 Combination Notes and the Class S2 Combination Notes shown above.

Secured by a Portfolio of Asset Backed Securities managed by Gulf International Bank (UK) Limited

FAB UK 2004-1 Limited, (incorporated in Jersey with limited liability under registered number 87004) (the "Issuer") will issue £157,500,000 Class A-1E Floating Rate Notes due 2045 (the "Class A-1E Notes"), £7,500,000 Class A-1F Zero Coupon Notes due 2045 (the "Class A-1F Notes" and together with the Class A-1E Notes, the "Class A1 Notes"), £10,000,000 Class A-2E Floating Rate Notes due 2045 (the "Class A-2E Notes"), £8,800,000 Class A-3E Floating Rate Notes due 2045 (the "Class A-2E Notes"), £8,800,000 Class A-3E Floating Rate Notes due 2045 (the "Class A-2E Notes"), £8,800,000 Class A-3E Floating Rate Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Floating Rate Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Floating Rate Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Floating Rate Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Floating Rate Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Floating Rate Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Floating Rate Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Floating Rate Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Floating Rate Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Floating Rate Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Floating Rate Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Floating Rate Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Floating Rate Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Floating Rate Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Floating Rate Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Notes due 2045 (the "Class A-3E Notes"), £8,800,000 Class A-3E Notes due 2045 (the "Class A-3E Notes due 2

FAB UK 2004-1 Ltd. – Issued Notes in descending Order of Priority

| Class of Notes | Notional (GBP) | Issue Price (% of Notional) | Interest |
|---------------------------|-------------------|---------------------------------------|---------------------------------|
| A-1E | 157.500.00 | 100% | 6m Libor + 0,5% |
| A-1F Zero | 7.500.000 | 65,66% | 6m Libor + 0,5%* |
| A-2E | 10.000.000 | 100% | 6m Libor + 0,8% |
| A-3E | 8.800.000 | 100% | 6m Libor + 1,1% |
| A-3F | 4.700.000 | 100% | 6,155% |
| BE | 9.000.000 | 100% | 6m Libor + 3,0% |
| С | 7.000.000 | 100% | 10% + Class C Residual Interest |
| Total Notional | 204.500.000 | | |
| Total Net Proceeds | | 201.924.560 | |

Transaction has many "tranches" with different risk-return-profile.

* Interest paid only after a certain date.

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» Data from investor report Dec. 2013:

| Security Name | ISIN | Туре | Principal Balance | Curr | Fitch | S&P | Payment | Index | Spread | Maturity |
|---|--------------|------|-------------------|------|-------|--------|-----------|-----------|------------|------------|
| ALBA 2005-1 - C Libor + 0.6% 11/2042 | XS0235713822 | RMBS | 1.453.035,92 | GBP | BBB- | BBB- | Quarterly | GBPLIBOR3 | 0,60% | 25.11.2042 |
| ALBA 2005-1 - Class D + 1.00% - 11/2042 | XS0235715363 | RMBS | 799.095,56 | GBP | B- | BB | Quarterly | GBPLIBOR3 | 1,00% | 25.11.2042 |
| ALBA 2007-1 - E Libor+1.2% - 01/2039 | XS0301708573 | RMBS | 4.500.000,00 | GBP | В | В | Quarterly | GBPLIBOR3 | 1,20% | 17.01.2039 |
| ALBA20062 - E Libor+0.95% 06/2038 | XS0271531435 | RMBS | 3.119.130,00 | GBP | В | В | Quarterly | GBPLIBOR3 | 0,95% | 15.06.2038 |
| AUBN3 - M Gbplibor+1.25% - 11/2039 | XS0157588723 | ABS | 2.500.000,00 | GBP | AA | AA- | Monthly | GBPLIBOR1 | 1,25% | 01.11.2039 |
| AUBN4 - D Gbplibor+1.05% - 10/2041 | XS0202812276 | ABS | 4.000.000,00 | GBP | A- | BBB | Monthly | GBPLIBOR1 | 1,05% | 01.10.2041 |
| AUBN4 - E Gbplibor+3.20% - 10/2041 | XS0202812516 | ABS | 3.500.000,00 | GBP | BB+ | BB- | Monthly | GBPLIBOR1 | 3,20% | 01.10.2041 |
| BLSuperFin - Floating - 10/2015 | XS0244893375 | CMBS | 66.720,04 | GBP | BBB | BBB | Quarterly | GBPLIBOR3 | 0,85% | 04.10.2015 |
| BRNL 2007-1X - A4B +0.11 Floating - 01/2039 | XS0289303215 | RMBS | 7.500.000,00 | GBP | AAA | A+ | Quarterly | GBPLIBOR3 | 0,11% | 13.01.2039 |
| BUMF1 - B Libor+4.75% 07/2036 | XS0186221577 | CMBS | 1.412.322,28 | GBP | AA | A- | Quarterly | GBPLIBOR3 | 4,75% | 20.07.2036 |
| BUMF2 - B Gbplibor+2.80% - 02/2037 | XS0203851463 | CMBS | 2.500.000,00 | GBP | Α | BBB | Quarterly | GBPLIBOR3 | 2,80% | 15.02.2037 |
| BUMF5 - B1 Libor+2.25% 02/2039 | XS0271325291 | CMBS | Accol | | | | No. of | | % of Outot | |
| DECO 2007-C4X - Class E + 1.00% - 01/2020 | XS0289644808 | CMBS | ASSel | Gla | 22 | NO. 01 | | | | SL. 020 |
| ECLIP 2006-4 - D GBPLibor + 0.62 - 10/2018 | XS0276413183 | CMBS | | | | S | ecurities | | Notional | |
| EPICP MLDN - Floating - 07/2017 Class D | XS0251156781 | CMBS | | | | | 00 | | 40 50/ | 017 |
| ERF 4 - Class C Libor +1.65% 07/2049 | XS0197424236 | ABS | RMBS | | | | 30 | | 46,5% | 049 |
| ERF 5 - C Libor+0.9% 07/2050 | XS0225884278 | RMBS | 01400 | | | | 10 | | 00.00/ | 050 |
| ERF3 - B Gbplibor+1.40% - 04/2038 | XS0169951000 | CMBS | CMBS | | | 18 | | | 30,6% | |
| FLEX 4 - A Gbplibor+0.27% - 07/2036 | XS0132692384 | RMBS | 4.5.0 | | | | 0 | | 47.00/ | 036 |
| FLEVE D.C | XS0149246711 | RMBS | ABS | | | | 9 | | 17,0% | 034 |
| | | | CDO | | | | 2 | | 5,9% | |
| | | | Total | | | | 59 | | 100,00% | 6 |

The collateral portfolio is very diverse (risk, maturity, payment frequencies, spreads).

FAB UK 2004-1 Ltd. – Schematic View of Transaction Triggers



Trigger mechanisms are designed to protect senior notes of the transaction.

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FAB UK 2004-1 Ltd. – Pre-Enforcement Priority of Payments – Interest

(A) payment of accrued and unpaid Trustee Fees and Expenses up to an amount equal to £35,000;

(B) payment, pari passu and pro rata (i) accrued and unpaid Administrative Expenses up to an amount equal to £125,000; (ii) any statutory fees or taxes (iii) an annual dividend not exceeding £500 per annum; and (iv) into the Expense Reimbursement Account of an amount equal to £20,000;

(C) payment of the Senior Collateral Management Fee

(D) pari passu and pro rata scheduled payments and any termination payments under the Hedge Agreement and Cap Agreement (only applies until 6.6.2012)

(E) payment of interest due and payable, pari passu and pro rata, in respect of the **Class A-1E Notes** and (where applicable) the **Class A-1F Notes** (if not redeemed on or prior to the Class A-1F Target Date);

(F) payment of interest due and payable, pro rata, in respect of the Class A-2E Notes;

(G) payment of interest due and payable, pari passu and pro rata, in respect of the Class A-3E Notes and the Class A-3F Notes;

(H) in the event of an early **redemption** by reason of a breach of the **Class A Coverage Test** and/or **Interest Coverage Test**, redemption, pari passu and pro rata, the **Class A-1E Notes** and the **Class A-1F Notes** and thereafter to redemption, pro rata, the **Class A-2E Notes** and thereafter redemption, pari passu and pro rata, the **Class A-3E Notes** and the **Class A-3E Notes**, to the extent necessary to cause the Class A Coverage Test and/or Interest Coverage Test to be met;

(I) payment of the Base Collateral Management Fee

(1) nevment of interest due and payable, pro rata, in respect of the Class BE Notes (including any interest on Class BE

FAB UK 2004-1 Ltd. – Coverage Tests and Event of Default

| Test | Calculation method* | Condition |
|------------------------------------|---|-----------|
| Class A Overcollateralization Test | (Outstanding Principal Portfolio + Repayments in excess of Class A Interest Coverage) / Outstanding Principal Class A | ≥ 103,5% |
| Class B Overcollateralization Test | (Outstanding Principal Portfolio + Repayments in excess of Class A+B Interest Coverage) / (Outstanding Principal Class A + B) | ≥ 101,0% |
| Interest Coverage Tests | 2 * (Annualized Interest Proceeds - Annualized Interest due for Class A) / Outstanding Principal Class A | ≥ 1,0% |
| Additional Coverage Test | See Class B OC Test | ≥ 101,5% |

- » Outcome of Coverage Tests determines certain steps of "Pre-enforcement" waterfall
- » Event of Default
 - Occurs IF Interest on the most senior note with nominal outstanding is not paid at a payment date (with the exception of Class C Note) OR if there is outstanding principal at maturity
 - > Default triggers sale of collateral portfolio and switch to "Post-enforcement" waterfall

Waterfall is determined by portfolio performance (indicated by Coverage Tests and Event of Default).

* Some simplifications were made.

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Case Study – FAB UK 2004-1 Ltd. – Revaluation Results

Background and Methodology

- » "MoCo" (Model Consolidation) Library is d-fine's internal valuation library
- » It can price a wide range of products (also structured credit securitizations)
- » Used at many customers for both validating and production environment
- » Validated by third parties and used in a production environment

Valuation of Structured Credit Securitizations

- » MoCo Modeling Language (MoML): Build into MoCo to allow the modeling of structured credit securitizations (waterfalls, triggers, tranches, portfolio)
- » Modeling is based on estimate of future cash flows
- » Excel Interface
- » System provides full transparency (all figures are exposed and can be validated manually)

d-fine's valuation capabilities cover nearly any level of complexity.

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d-fine's Approach to value Structured Credit Securitizations



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FAB UK 2004-1 Ltd. – Modeling Approach for ABS Reference Portfolio

Main Challenge: Modeling cash flows of ABS CDO tranches in the reference portfolio

- » Important information that was not available:
 - > Default rates/ expected losses
 - > Redemption schedules
 - > Prepayment assumptions

Portfolio Modeling Approach:

- » Modeling ABS CDOs like individual loans using the following assumptions:
 - > Annuity repayment profile as mortgages typically repay in annuities
 - > Probability of default based on historical default rates for the S&P rating given in latest investor report
 - > Recovery rate based on recovery assumptions from Offering Circular (Junior tranches)
 - > Zero prepayments, as they were not mentioned in the investor reports
- » Alternative approach:
 - > Modeling all 59 underlyings explicitly using deal information and investor reports \rightarrow unreasonable effort

Chosen approach is reasonable trade-off between model simplification and valuation accuracy.

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FAB UK 2004-1 Ltd. – Assumptions for Credit Quality of Reference Portfolio

| S&P Rating | Historical Default Rate | Notional by Rating | Portion of Total Notional |
|------------|----------------------------|-----------------------|------------------------------|
| AAA | 0,04% | 446.414,88 | 0,3% |
| AA | 0,09% | 7.029.532,75 | 5,0% |
| А | 0,17% | 35.080.286,04 | 24,8% |
| BBB | 0,50% | 29.784.686,30 | 21,1% |
| BB | 3,52% | 12.643.039,16 | 9,0% |
| В | 3,32% | 36.263.230,04 | 25,7% |
| CCC | 16,14% | 3.800.494,25 | 2,7% |
| CC | 35,34% | - | 0,0% |
| С | 35,34% | 2.000.000,00 | 1,4% |
| D | 100,00% | 8.158.127,42 | 5,8% |
| NR | 50,00%* | 6.000.000,00 | 4,2% |
| | | 141.205.810,84 | 100% |

> Example: first-year **expected loss** for a AA-rated security with notional of GBP 1000: $EAD \cdot LGD \cdot PD = 1000 \cdot (1 - 0.55) \cdot 0.0009 = 0.405$

Default rates taken from RatingsDirect Report by S&P; Recovery rates taken from the transaction's offering circular. (* Own assumption)

FAB UK 2004-1 Ltd. – Transaction Specific Valuation Approach

Summary of the valuation approach:

- » Reference Portfolio
 - > Remodeling ABS tranches as synthetic loans
 - Use historic rating performances as information about credit quality
- » Modeling specific features of transaction
 - Identify and model relevant steps of waterfall
 - Modeling of coverage tests
 - Make reasonable simplifications: substitution of collateral, optional redemption, IRS
- » Simulate different scenarios of portfolio performance
- » Calculate Present Values for tranches

FAB UK 2004-1 Ltd. – Cash Flow Tables Reference Portfolio

| | Cashflows for Re | ferencePortfolio | | | | | |
|----------|------------------|------------------|----------------|------------|---------------|--------------|----------------|
| eference | RefPortList | | | | | | |
| /alDate | 31.12.2013 | | | | Check OK | | |
| | Totals | 70.830.871,00 | 106.870.903,64 | - | 34.334.907,20 | 1.741.465,12 | 32.593.442,08 |
| | PayDate | Interest | Principal | Prepayment | Default | Recovery | RealizedLosses |
| | 20.10.2010 | 1,00 | 0,00 | 0,00 | 0,00 | 0,00 | 0,00 |
| | 22.10.2012 | 0,00 | 0,00 | 0,00 | 0,00 | 0,00 | 0,00 |
| | 31.01.2014 | 44.487,80 | 72.171,30 | 0,00 | 216.759,02 | 0,00 | 0,00 |
| | 28.02.2014 | 39.680,64 | 75.770,81 | 0,00 | 189.206,10 | 0,00 | 0,00 |
| | 31.03.2014 | 591.417,82 | 2.191.672,39 | 0,00 | 2.174.198,74 | 0,00 | 0,00 |
| | 30.04.2014 | 41.759,20 | 71.193,74 | 0,00 | 189.106,50 | 0,00 | 0,00 |
| | 02.06.2014 | 45.166,30 | 66.506,46 | 0,00 | 200.627,30 | 0,00 | 0,00 |
| | 30.06.2014 | 592.579,83 | 2.577.703,75 | 0,00 | 1.855.161,19 | 0,00 | 0,00 |
| | 31.07.2014 | 42.234,50 | 67.267,14 | 0,00 | 175.898,24 | 0,00 | 0,00 |
| | 01.09.2014 | 42.886,78 | 65.497,44 | 0,00 | 175.173,73 | 0,00 | 0,00 |
| | 30.09.2014 | 606.136,09 | 2.013.407,76 | 0,00 | 1.600.290,59 | 0,00 | 0,00 |
| | 20.10.2014 | 0,00 | 0,00 | 0,00 | 0,00 | 0,00 | 0,00 |
| | 31.10.2014 | 40.964,77 | 65.431,50 | 0,00 | 158.360,80 | 0,00 | 0,00 |
| | 01.12.2014 | 40.326,83 | 65.094,54 | 0,00 | 152.885,91 | 0,00 | 0,00 |
| | 31.12.2014 | 627.909,11 | 2.409.139,68 | 0,00 | 1.384.371,71 | 0,00 | 0,00 |
| | 02.02.2015 | 49.868,51 | 53.674,50 | 0,00 | 151.702,20 | 2.096,04 | 214.662,98 |
| | 02.03.2015 | 41.696,72 | 61.053,09 | 0,00 | 124.435,74 | 1.883,48 | 187.322,63 |
| | 31.03.2015 | 667.928,31 | 1.846.441,23 | 0,00 | 1.166.744,44 | 30.870,46 | 2.143.328,28 |
| | 30.04.2015 | 43.506,28 | 57.652,52 | 0,00 | 124.867,30 | 1.996,72 | 187.109,78 |
| | 01.06.2015 | 45.790,08 | 54.548,85 | 0,00 | 128.671,35 | 0,00 | 0,00 |
| | 02.06.2015 | 0,00 | 0,00 | 0,00 | 0,00 | 2.184,69 | 198.442,61 |
| | 30.06.2015 | 658.206,40 | 2.294.447,72 | 0,00 | 1.030.103,78 | 32.153,42 | 1.823.007,77 |
| | 31.07.2015 | 43.201,87 | 55.676,46 | 0,00 | 116.540,34 | 2.030,81 | 173.867,43 |
| | 01.09.2015 | 44.016,04 | 54.122,26 | 0,00 | 116.192,34 | 2.085,31 | 173.088,42 |
| | 30.09.2015 | 747.772.85 | 1.699.128,81 | 0,00 | 907 009 41 | 30.150,02 | 1.570.140.57 |

MoCo MoML allows a view on all portfolio cash flows (on an aggregated level).

FAB UK 2004-1 Ltd. – Cash Flows Reference Portfolio (Base Case)



» Total expected realized losses are around 23% (of total nominal)

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FAB UK 2004-1 Ltd. – Cash Flow Tables Tranches

| Cashflows for Tranche XS0187362104_Amount ClassA-1E | | Calculate | | | | WAL Non-disc. CFs Non-disc. CFs / Nom. | 8,93 112.613.759,37 134% | | | | | |
|---|------------|------------|------------|-----------|---------------|--|--------------------------------|--------------|--------|--------------|------|--------------|
| Per_beg | Per_end | Pay_dat | Fix_dat | Year.frac | 'non-disc' PV | Nom. | Outst.Nom | Coupon | rate | I-Paymt | CID | P-Paymt |
| 00.01.1900 | 31.12.2013 | 31.12.2013 | 31.12.2013 | 0,0000 | 0,00 | 84.295.503,36 | 84.295.503,36 | 0,00 | 0,00 | 0,00 | 0,00 | 0,00 |
| 31.12.2013 | 06.06.2014 | 06.06.2014 | 04.06.2014 | 0,4301 | 2.826.111,38 | 84.295.503,36 | 81.930.793,87 | 461.401,89 | 0,0127 | 461.401,89 | 0,00 | 2.364.709,49 |
| 06.06.2014 | 08.12.2014 | 08.12.2014 | 04.12.2014 | 0,5068 | 5.461.524,77 | 81.930.793,87 | 77.127.249,61 | 657.980,51 | 0,0158 | 657.980,51 | 0,00 | 4.803.544,26 |
| 08.12.2014 | 08.06.2015 | 08.06.2015 | 04.06.2015 | 0,4986 | 5.224.626,68 | 77.127.249,61 | 72.666.914,85 | 764.291,92 | 0,0199 | 764.291,92 | 0,00 | 4.460.334,75 |
| 08.06.2015 | 07.12.2015 | 07.12.2015 | 03.12.2015 | 0,4986 | 5.090.300,17 | 72.666.914,85 | 68.545.501,79 | 968.887,11 | 0,0267 | 968.887,11 | 0,00 | 4.121.413,07 |
| 07.12.2015 | 06.06.2016 | 06.06.2016 | 02.06.2016 | 0,4986 | 5.346.320,87 | 68.545.501,79 | 64.152.528,36 | 953.347,44 | 0,0279 | 953.347,44 | 0,00 | 4.392.973,42 |
| 06.06.2016 | 06.12.2016 | 06.12.2016 | 02.12.2016 | 0,5014 | 4.037.647,53 | 64.152.528,36 | 61.207.195,90 | 1.092.315,07 | 0,0340 | 1.092.315,07 | 0,00 | 2.945.332,46 |
| 06.12.2016 | 06.06.2017 | 06.06.2017 | 02.06.2017 | 0,4986 | 3.855.890,10 | 61.207.195,90 | 58.421.622,71 | 1.070.316,92 | 0,0351 | 1.070.316,92 | 0,00 | 2.785.573,19 |
| 06.06.2017 | 06.12.2017 | 06.12.2017 | 04.12.2017 | 0,5014 | 3.763.269,79 | 58.421.622,71 | 55.802.171,66 | 1.143.818,74 | 0,0391 | 1.143.818,74 | 0,00 | 2.619.451,05 |
| 06.12.2017 | 06.06.2018 | 06.06.2018 | 04.06.2018 | 0,4986 | 3.248.497,89 | 55.802.171,66 | 53.657.956,34 | 1.104.282,57 | 0,0397 | 1.104.282,57 | 0,00 | 2.144.215,32 |
| 06.06.2018 | 06.12.2018 | 06.12.2018 | 04.12.2018 | 0,5014 | 3.300.667,76 | 53.657.956,34 | 51.482.546,85 | 1.125.258,27 | 0,0418 | 1.125.258,27 | 0,00 | 2.175.409,49 |
| 06.12.2018 | 06.06.2019 | 06.06.2019 | 04.06.2019 | 0,4986 | 2.698.945,80 | 51.482.546,85 | 49.866.970,66 | 1.083.369,61 | 0,0422 | 1.083.369,61 | 0,00 | 1.615.576,19 |
| 06.06.2019 | 06.12.2019 | 06.12.2019 | 04.12.2019 | 0,5014 | 2.656.227,58 | 49.866.970,66 | 48.297.464,83 | 1.086.721,75 | 0,0435 | 1.086.721,75 | 0,00 | 1.569.505,83 |
| 06.12.2019 | 08.06.2020 | 08.06.2020 | 04.06.2020 | 0,5068 | 2.622.018,11 | 48.297.464,83 | 46.744.822,24 | 1.069.375,52 | 0,0437 | 1.069.375,52 | 0,00 | 1.552.642,59 |
| 08.06.2020 | 07.12.2020 | 07.12.2020 | 03.12.2020 | 0,4986 | 2.595.549,73 | 46.744.822,24 | 45.199.610,44 | 1.050.337,94 | 0,0451 | 1.050.337,94 | 0,00 | 1.545.211,80 |
| 07.12.2020 | 07.06.2021 | 07.06.2021 | 03.06.2021 | 0,4986 | 2.570.873,37 | 45.199.610,44 | 43.650.062,79 | 1.021.325,72 | 0,0453 | 1.021.325,72 | 0,00 | 1.549.547,65 |
| 07.06.2021 | 06.12.2021 | 06.12.2021 | 02.12.2021 | 0,4986 | 2.542.594,78 | 43.650.062,79 | 42.111.517,38 | 1.004.049,37 | 0,0461 | 1.004.049,37 | 0,00 | 1.538.545,41 |
| 06.12.2021 | 06.06.2022 | 06.06.2022 | 02.06.2022 | 0,4986 | 2.521.213,22 | 42.111.517,38 | 40.562.265,23 | 971.961,07 | 0,0463 | 971.961,07 | 0,00 | 1.549.252,14 |
| 06.06.2022 | 06.12.2022 | 06.12.2022 | 02.12.2022 | 0,5014 | 2.497.061,38 | 40.562.265,23 | 39.011.925,47 | 946.721,61 | 0,0466 | 946.721,61 | 0,00 | 1.550.339,77 |
| 06.12.2022 | 06.06.2023 | 06.06.2023 | 02.06.2023 | 0,4986 | 2.482.010,83 | 39.011.925,47 | 37.436.556,13 | 906.641,49 | 0,0466 | 906.641,49 | 0,00 | 1.575.369,34 |
| 06.06.2023 | 06.12.2023 | 06.12.2023 | 04.12.2023 | 0,5014 | 2.434.221,73 | 37.436.556,13 | 35.887.459,63 | 885.125,23 | 0,0472 | 885.125,23 | 0,00 | 1.549.096,50 |
| 06.12.2023 | 06.06.2024 | 06.06.2024 | 04.06.2024 | 0,5014 | 2.414.617,31 | 35.887.459,63 | 34.322.920,00 | 850.077,67 | 0,0472 | 850.077,67 | 0,00 | 1.564.539,64 |
| 06.06.2024 | 06.12.2024 | 06.12.2024 | 04.12.2024 | 0,5014 | 2.400.195,21 | 34.322.920,00 | 32.735.700,93 | 812.976,15 | 0,0472 | 812.976,15 | 0,00 | 1.587.219,06 |
| 06.12.2024 | 06.06.2025 | 06.06.2025 | 04.06.2025 | 0,4986 | 2.388.868,13 | 32,735,700,93 | 31.118.016,49 | 771.183,69 | 0,0472 | 771.183,69 | 0,00 | 1.617.684,44 |
| 06.06.2025 | 08.12.2025 | 08.12.2025 | 04.12.2025 | 0,5068 | 2.364.609,50 | 31.118.016,49 | 29.482.389,72 | 728.982,74 | 0,0462 | 728.982,74 | 0,00 | 1.635.626,77 |
| 08.12.2025 | 08.06.2026 | 08.06.2026 | 04.06.2026 | 0,4986 | 2.362.580,43 | 29.482.389,72 | 27.796.689,63 | 676.880,34 | 0,0460 | 676.880,34 | 0,00 | 1.685.700,09 |
| 08.06.2026 | 07.12.2026 | 07.12.2026 | 03.12.2026 | 0,4986 | 2.350.346,48 | 27.796.689,63 | 26.084.490,07 | 638.146,92 | 0,0460 | 638.146,92 | 0,00 | 1.712.199,56 |
| 07.12.2026 | 07.06.2027 | 07.06.2027 | 03.06.2027 | 0,4986 | 2.338.338,29 | 26.084.490,07 | 24.345.020,43 | 598.868,64 | 0,0460 | 598.868,64 | 0,00 | 1.739.469,65 |
| 07.06.2027 | 06.12.2027 | 06.12.2027 | 02.12.2027 | 0,4986 | 2.327.289,97 | 24.345.020,43 | 22.576.662,96 | 558.932,50 | 0,0460 | 558.932,50 | 0,00 | 1.768.357,47 |
| 06.12.2027 | 06.06.2028 | 06.06.2028 | 02.06.2028 | 0,5014 | 2.313.185,10 | 22.576.662,96 | 20.784.710,87 | 521.233,01 | 0,0460 | 521.233,01 | 0,00 | 1.791.952,09 |
| 06.06.2028 | 06.12.2028 | 06.12.2028 | 04.12.2028 | 0,5014 | 2.323.724,83 | 20.784.710,87 | 18.917.120,51 | 456.134,48 | 0,0438 | 456.134,48 | 0,00 | 1.867.590,36 |
| 06.12.2028 | 06.06.2029 | 06.06.2029 | 04.06.2029 | 0,4986 | 2.320.672,90 | 18.917.120,51 | 17.005.939,50 | 409.491,89 | 0,0434 | 409.491,89 | 0,00 | 1.911.181,01 |
| 06.06.2029 | 06.12.2029 | 06.12.2029 | 04.12.2029 | 0,5014 | 2.309.028,85 | 17.005.939,50 | 15.067.037,44 | 370.126,79 | 0,0434 | 370.126,79 | 0,00 | 1.938.902,06 |
| 06.12.2029 | 06.06.2030 | 06.06.2030 | 04.06.2030 | 0,4986 | 2.278.739,87 | 15.067.037,44 | 13.114.448,15 | 326.150,57 | 0,0434 | 326.150,57 | 0,00 | 1.952.589,30 |
| 06.06.2030 | 06.12.2030 | 06.12.2030 | 04.12.2030 | 0,5014 | 1.988.196,07 | 13.114.448,15 | 11.411.682,27 | 285.430,19 | 0,0434 | 285.430,19 | 0,00 | 1.702.765,88 |
| 0.0 10 | | 00.00 | 04 06 2031 | 0.4986 | 2.014.251.20 | 11.411.682.27 | 0.011.10 | | 0.0494 | 247 024 45 | 0.00 | 1.767.226.74 |

MoCo MoML allows a view on all tranche cash flows.

FAB UK 2004-1 Ltd. – Principal Cash Flows to Notes (Base Case)



- » Senior tranches are expected to be redeemed long before their legal maturity (2045)
- » The two lowest tranches are not expected to receive any principal payments

FAB UK 2004-1 Ltd. – Interest Cash Flows to Notes (Base Case)



- » Exp. interest payments are driven by shape of the forward curve and outstanding nominal
- » Class BE receives large interest cash flow from expected asset sale at maturity

FAB UK 2004-1 Ltd. – Reference Portfolio Assumptions under Stress Scenario

| S&P Rating | Historical Default Rate |
|------------|----------------------------|
| AAA | 0,10% |
| AA | 0,23% |
| А | 0,43% |
| BBB | 1,25% |
| BB | 8,80% |
| В | 8,30% |
| CCC | 40,35% |
| CC | 88,35% |
| С | 88,35% |
| D | 100,00% |
| NR | 100,00%* |

» Stress Scenario

- > Default rates increase by factor 2,5
- Recovery rates decrease by factor 0,5

Scenario is to test protection of senior tranches.

Default rates taken from RatingsDirect Report by S&P; Recovery rates taken from the transaction's offering circular. (* Own assumption)

2015-10-07 | Delocalised Niagara Falls in the Financial Industry | Real World Example (21/25)

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FAB UK 2004-1 Ltd. – Cash Flows Reference Portfolio (Stress Case)



» Total expected realized losses amount to around 34% (of total nominal)

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FAB UK 2004-1 Ltd. – Principal Cash Flows to Notes (Stress Case)



- » Senior tranches still redeem in full but later than in base case
- » The *four* lowest tranches are not expected to receive any principal payments

FAB UK 2004-1 Ltd. – Interest Cash Flows to Notes (Stress Case)



- » Class A1 interest payments stretch further as expected redemption is later
- » Classes BE and C do not receive any interest (or principal) payments

FAB UK 2004-1 Ltd. – Revaluation Results as of 31.12.2013

| Class of Notes | PV (Base Case, in %) | PV (Stress Case, in %) |
|----------------|--------------------------------|----------------------------------|
| A-1E | 104,89 | 105,41 |
| A-1F Zero | 104,89 | 105,41 |
| A-2E | 113,82 | 76,93 |
| A-3E | 119,78 | 30,99 |
| A-3F | 141,57 | 36,51 |
| BE | 1,84 | 0,00 |
| C | 0,00 | 0,00 |

» Present values reflect theoretical "fair value" based on expected cash flows

- > Senior notes' PV is very little affected by change in portfolio performance (to a certain point)
- > Mezzanine notes offer high return if portfolio performs normal
- » However, illiquidity can have major effect on actual realized price

True MtM would require knowledge of the actual demand-supply situation ("market color").

Contact

Dr Samuel Tebege

| Manager | |
|---------|-------------------------|
| Tel | +49 89-7908617-147 |
| Mobile | +49 162-263-0063 |
| E-Mail | samuel.tebege@d-fine.de |

d-fine GmbH

Frankfurt München London Wien Zürich

Zentrale

d-fine GmbH Opernplatz 2 D-60313 Frankfurt/Main

Tel +49 69-90737-0 Fax +49 69-90737-200

www.d-fine.com

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