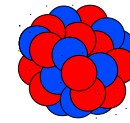
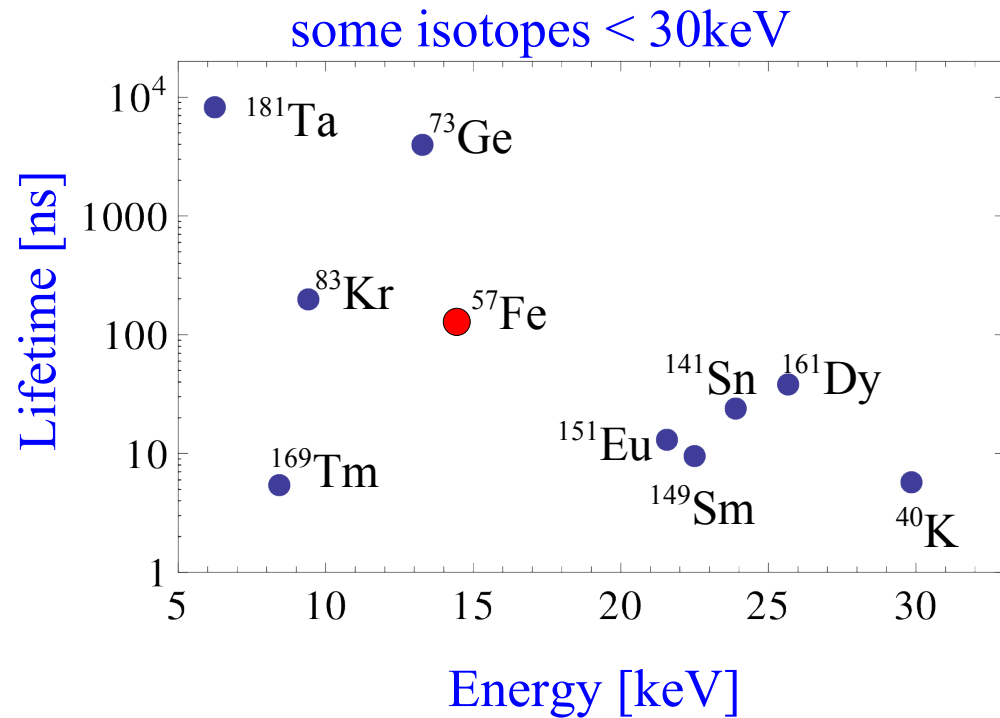
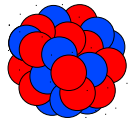
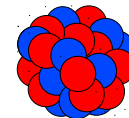


Nuclear quantum optics

Nuclear transition energies

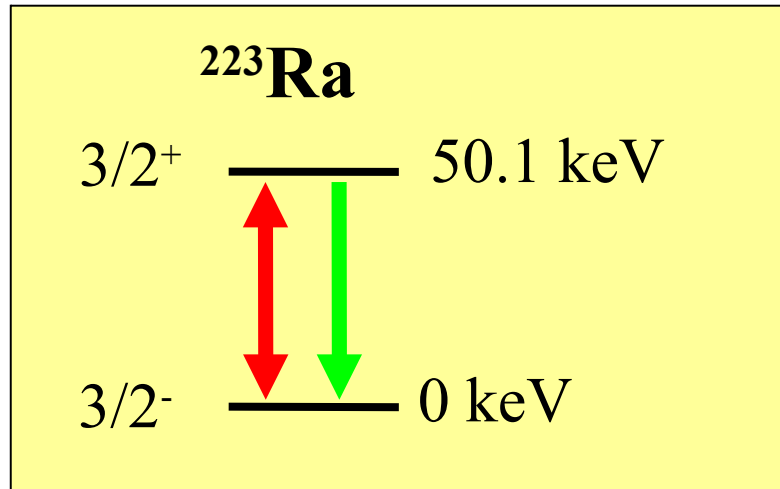


but many more with higher energies – use target acceleration!



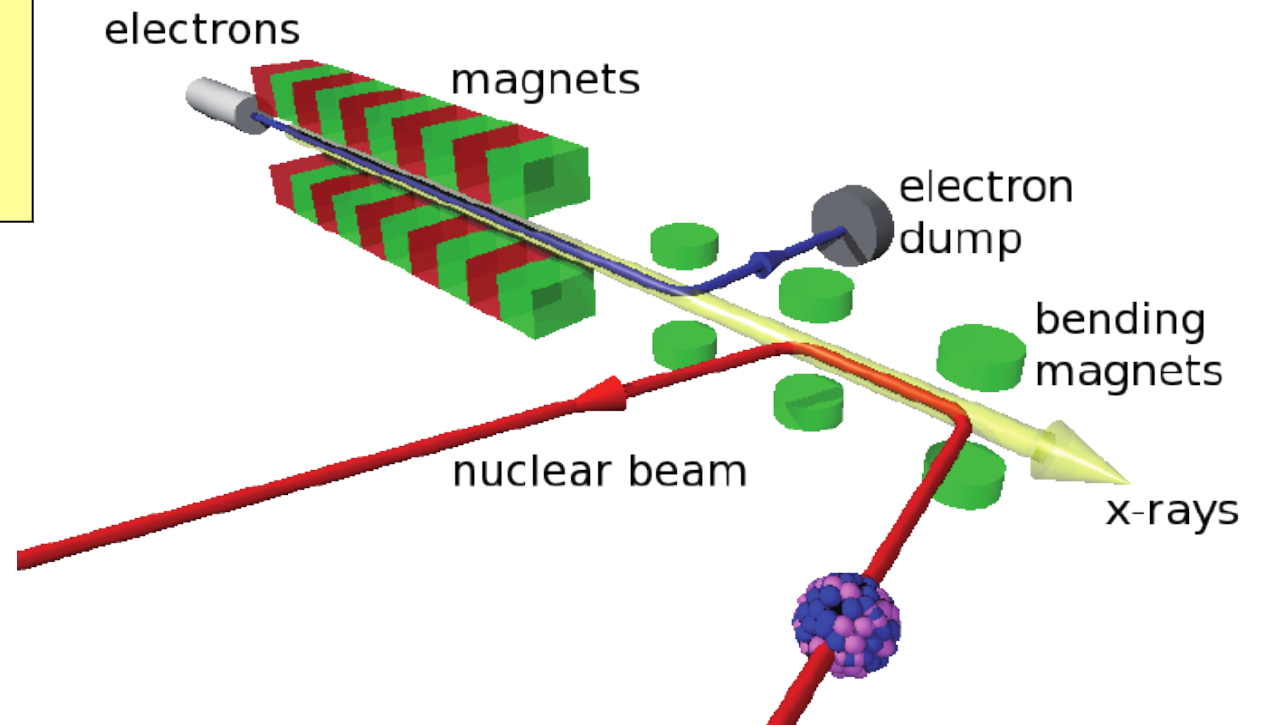
Accelerated nuclei as targets

bridge the gap between nuclear excitation and photon energies...



Doppler shift

$$E_n = (1 + \beta)\gamma E_L$$



Accelerated nuclei as targets

bridge the gap between nuclear excitation and photon energies...

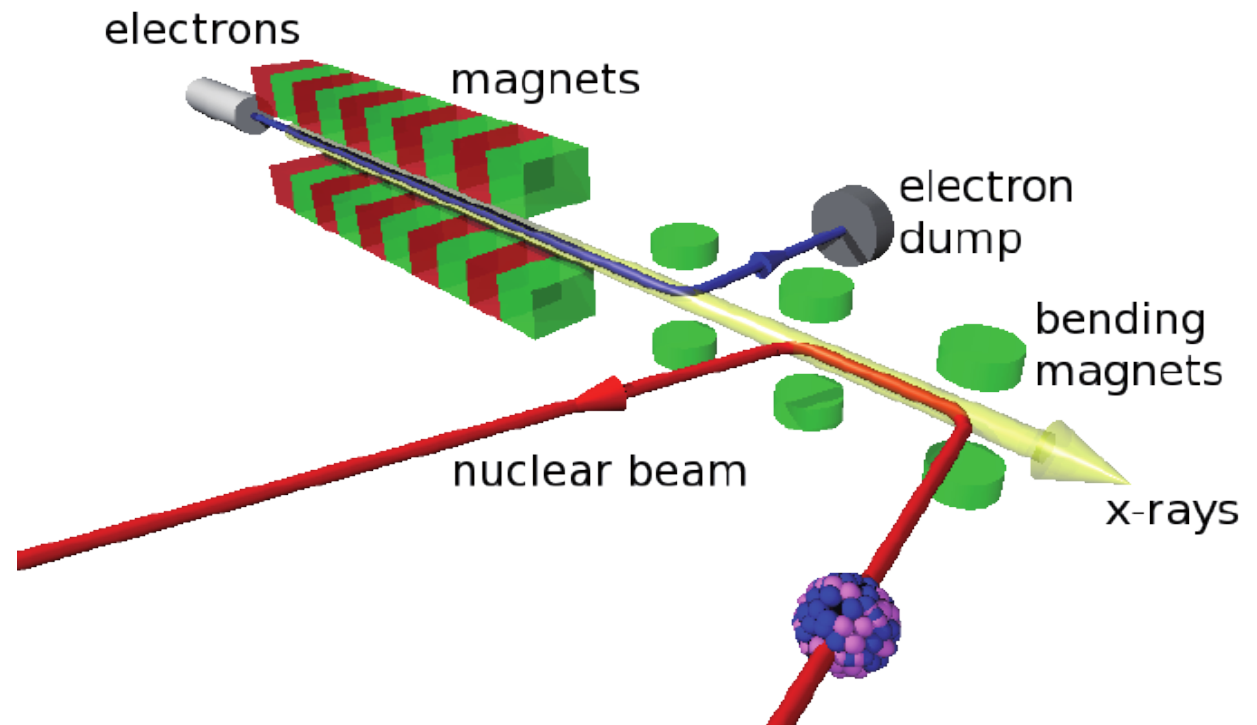
Doppler shift

$$\beta = \frac{v}{c} \quad \gamma = \frac{1}{\sqrt{1 - \beta^2}}$$

$$t_b = \frac{t_l}{(1 + \beta)\gamma}$$

$$I_b = I_l(1 + \beta)\gamma$$

$$E_b = E_n = (1 + \beta)\gamma E_l$$



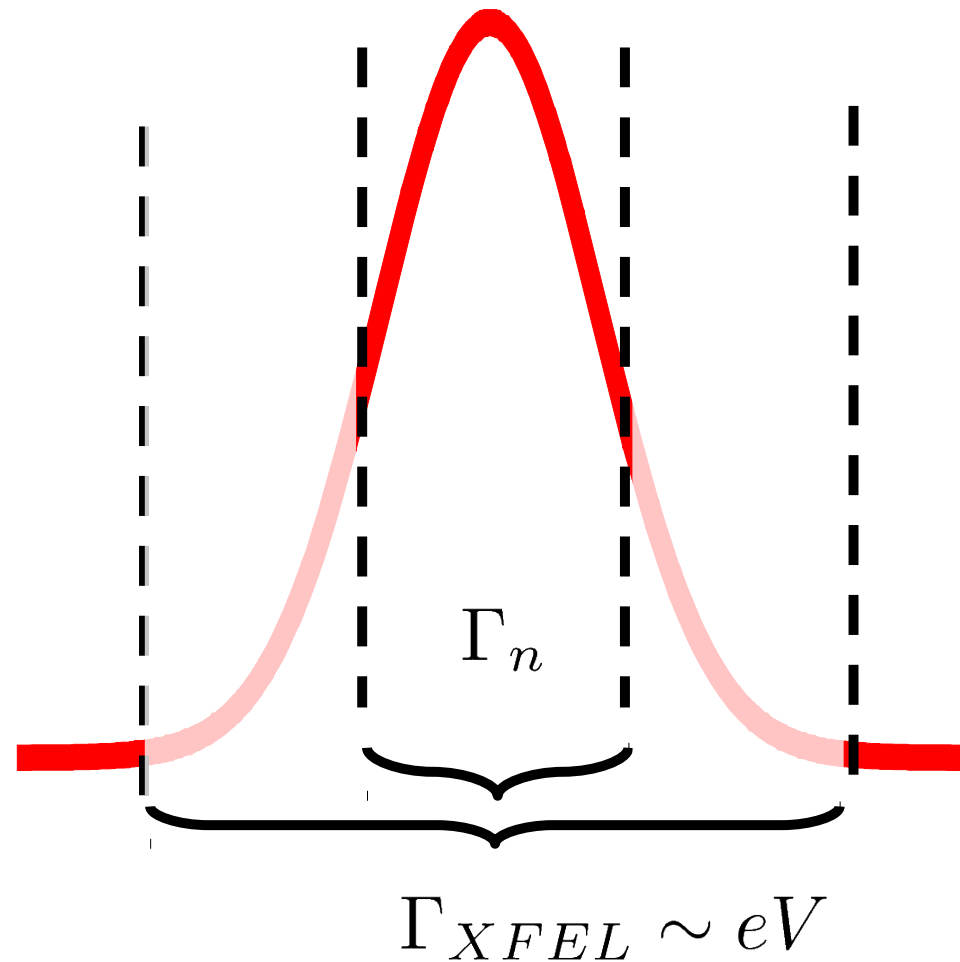
Nuclear transition widths

Nuclear widths are very narrow!

$$\Gamma_n \sim 10^{-8} - 10^{-5} \text{ eV}$$

$$I_{eff} = I \frac{\Gamma_n}{\Gamma_{XFEL}}$$

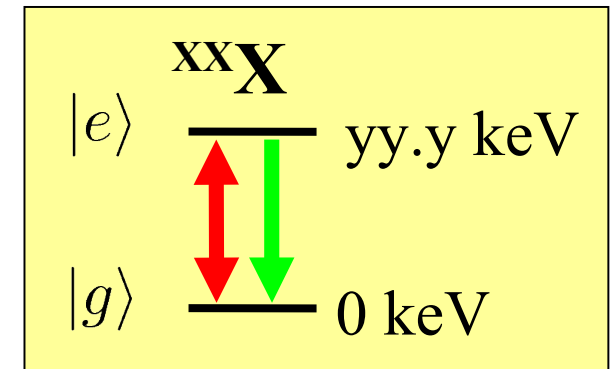
effective intensity!



Quantum optics approach

Density matrix formalism

$$\rho = |\Psi\rangle\langle\Psi| \quad |\Psi\rangle = c_g|g\rangle + c_e|e\rangle$$



→ so-called Bloch equations

$$\frac{\partial \rho}{\partial t} = -\frac{i}{\hbar} [H_0, \rho] - \underbrace{\frac{\gamma_{SE}}{2} (A_{eg}A_{ge}\rho + \rho A_{eg}A_{ge} - 2A_{ge}\rho A_{eg})}_{\text{spontaneous emission}}$$

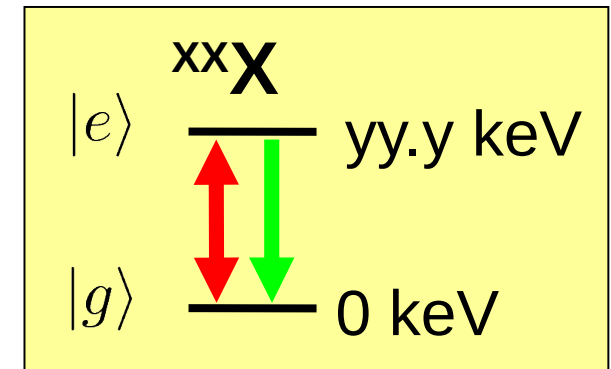
$$A_{ij} = |i\rangle\langle j|, \quad i, j \in \{e, g\}$$

$$H_0 = -\frac{1}{c} \int d^3r \vec{j}(\vec{r}) \cdot \vec{A}(\vec{r}, t)$$

Nuclear transition might be “forbidden”

Atomic quantum optics – electric dipole E1 transitions

Low-lying nuclear transitions - M1, E2, rarely E1



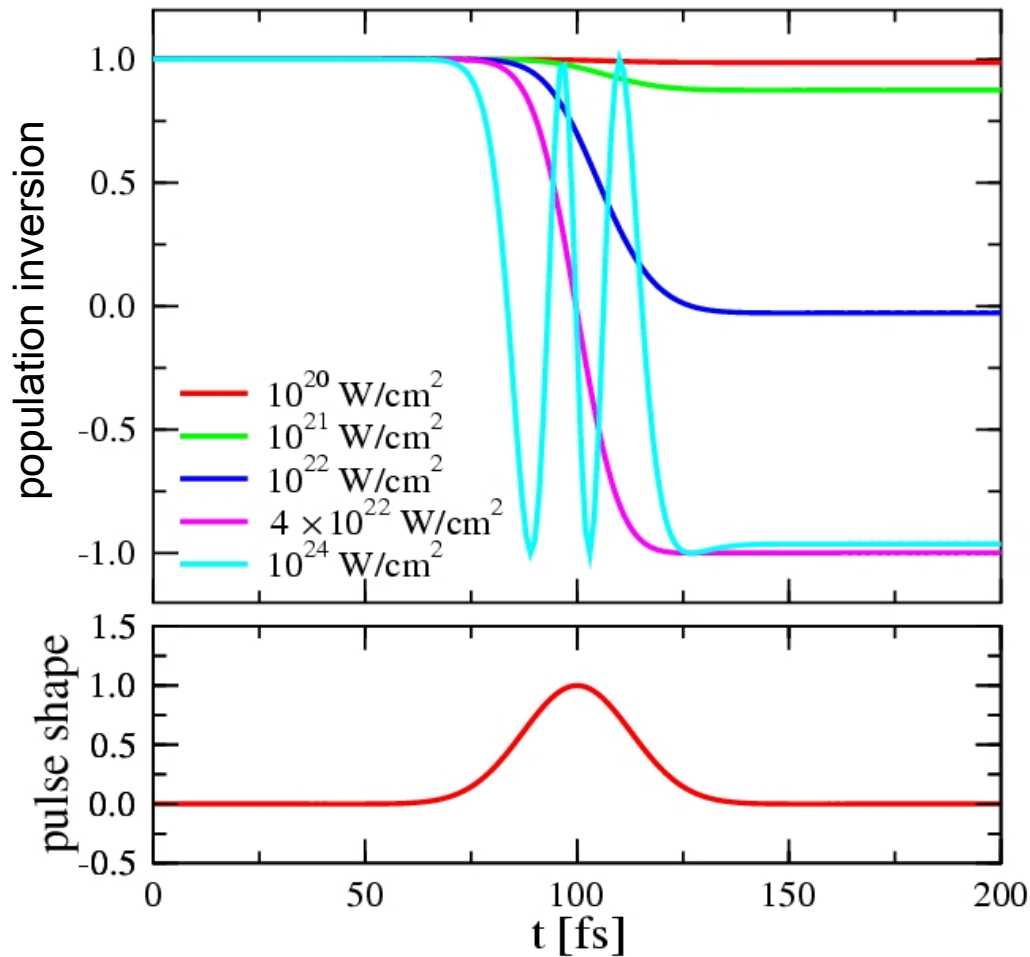
$$\frac{\partial \rho}{\partial t} = -\frac{i}{\hbar} [H_0, \rho] - \underbrace{\frac{\gamma_{SE}}{2} (A_{eg} A_{ge} \rho + \rho A_{eg} A_{ge} - 2 A_{ge} \rho A_{eg})}_{\text{spontaneous emission}}$$

Beyond the dipole approximation!

$$A_{ij} = |i\rangle\langle j|, \quad i, j \in \{e, g\}$$

$$H_0 = -\frac{1}{c} \int d^3r \vec{j}(\vec{r}) \cdot \vec{A}(\vec{r}, t) \propto \mathfrak{M}_{LM} \neq -e\vec{r} \cdot \vec{E}$$

Nuclear Rabi flopping



Population inversion in ^{223}Ra

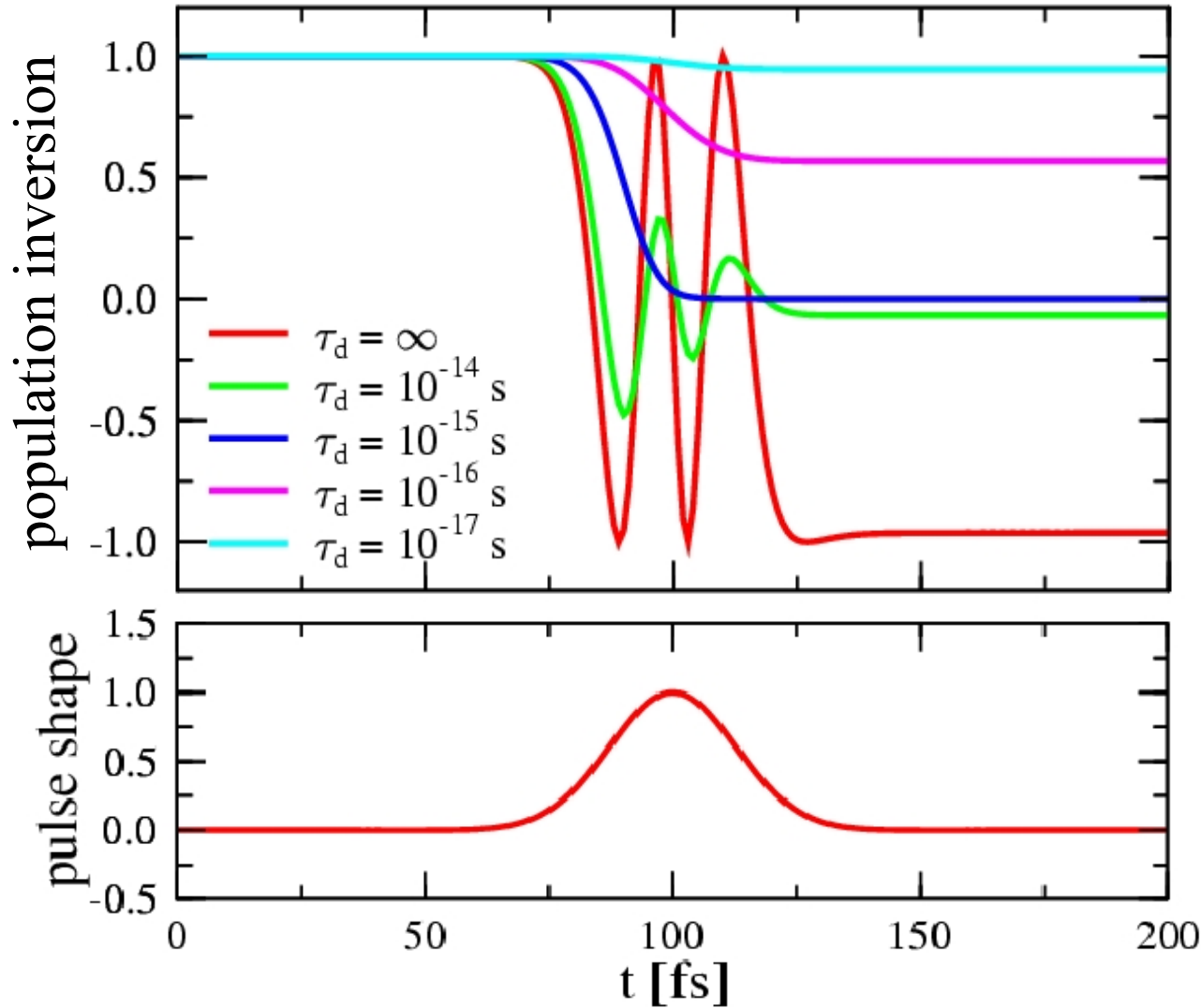
Population inversion \sim

$$\langle g|\rho|g\rangle - \langle e|\rho|e\rangle$$

- resonant laser-nucleus interaction allows to induce Rabi flopping of nuclear population
- detection e.g. via scattered light, state-selective measurements
- potential application: model-free determination of nuclear parameters

Coherence in nuclear Rabi flopping

coherence \longleftrightarrow intensity



strongly incoherent

partially coherent

coherent

Coherence in nuclear Rabi flopping

coherence \longleftrightarrow intensity

