

*Two level system semiclassically with spontaneous decay introduced phenomenologically  
 HGSP Graduate Days October 2018  
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Equations to solve:

1. Spontaneous decay from e to g

$$\begin{aligned} \frac{d}{dt} \rho_{ee} &= -\gamma * \rho_{ee} + i\Omega (\rho_{eg} - \rho_{ge}) \\ \frac{d}{dt} \rho_{gg} &= \gamma * \rho_{ee} - i\Omega (\rho_{eg} - \rho_{ge}) \\ \frac{d}{dt} \rho_{eg} &= (i\Delta - \gamma / 2) * \rho_{eg} + i\Omega (\rho_{ee} - \rho_{gg}) \\ \frac{d}{dt} \rho_{ge} &= (-i\Delta - \gamma / 2) * \rho_{ge} - i\Omega (\rho_{ee} - \rho_{gg}) \end{aligned}$$

Initially, the atom is in the ground state.

2. Spontaneous decay from e/g outside the system

$$\begin{aligned} \frac{d}{dt} \rho_{ee} &= -\gamma_e * \rho_{ee} + i\Omega (\rho_{eg} - \rho_{ge}) \\ \frac{d}{dt} \rho_{gg} &= -\gamma_g * \rho_{ee} - i\Omega (\rho_{eg} - \rho_{ge}) \\ \frac{d}{dt} \rho_{eg} &= (i\Delta - (\gamma_g + \gamma_e) / 2) * \rho_{eg} + i\Omega (\rho_{ee} - \rho_{gg}) \\ \frac{d}{dt} \rho_{ge} &= (-i\Delta - (\gamma_g + \gamma_e) / 2) * \rho_{ge} - i\Omega (\rho_{ee} - \rho_{gg}) \end{aligned}$$

Initially, the atom is in the ground state.

**Parameters**

```
OmegaRabi = 1;
GammaRate = 1;
GammaRateE = 1;
GammaRateG = 0.3;
Detuning = 0;
PulseDuration = 10;
```

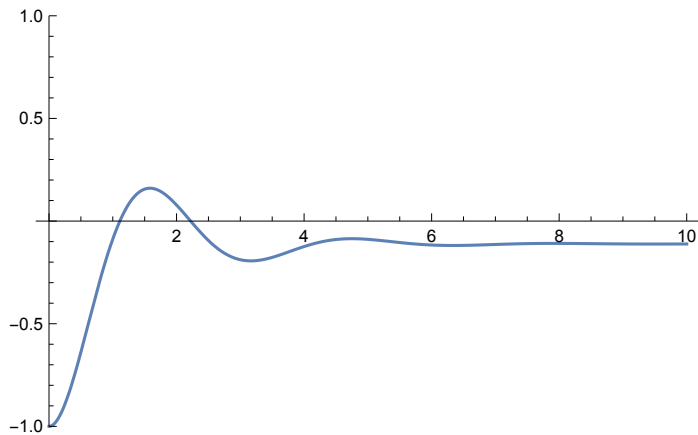
**The Bloch Equations System 1**

```
Eqns1 = {D[\rho_{gg}[t], t] == GammaRate * \rho_{ee}[t] - I * OmegaRabi *
(\rho_{eg}[t] - \rho_{ge}[t]),
D[\rho_{ge}[t], t] ==
-i * Detuning * \rho_{ge}[t] + i * OmegaRabi * (\rho_{gg}[t] - \rho_{ee}[t]) - GammaRate * \rho_{ge}[t] / 2,
D[\rho_{ee}[t], t] == -GammaRate * \rho_{ee}[t] + I * OmegaRabi * (\rho_{eg}[t] - \rho_{ge}[t]),
D[\rho_{eg}[t], t] == i * Detuning * \rho_{eg}[t] +
i * OmegaRabi * (\rho_{ee}[t] - \rho_{gg}[t]) - GammaRate * \rho_{eg}[t] / 2,
\rho_{gg}[0] == 1, \rho_{ee}[0] == 0, \rho_{ge}[0] == 0, \rho_{eg}[0] == 0};
```

```
ToSolve = {\rho_{gg}, \rho_{ee}, \rho_{ge}, \rho_{eg}};
```

```
sol1 = DSolve[Eqns1, ToSolve, t];
```

```
Plot[Re[ρee[t] /. sol1] - Re[ρgg[t] /. sol1],
{t, 0, PulseDuration}, PlotRange → {-1, 1}]
```



## The Bloch Equations System 2

```
Eqns2 = {D[ρgg[t], t] == -GammaRateG * ρgg[t] -
  I * OmegaRabi * (ρeg[t] - ρge[t]),
  D[ρge[t], t] == -i * Detuning * ρge[t] + i * OmegaRabi * (ρgg[t] - ρee[t]) -
  (GammaRateE + GammaRateG) * ρge[t] / 2,
  D[ρee[t], t] == -GammaRateE * ρee[t] + I * OmegaRabi * (ρeg[t] - ρge[t]),
  D[ρeg[t], t] == i * Detuning * ρeg[t] + i * OmegaRabi * (ρee[t] - ρgg[t]) -
  (GammaRateE + GammaRateG) * ρeg[t] / 2,
  ρgg[0] == 1, ρee[0] == 0, ρge[0] == 0, ρeg[0] == 0};
```

```
ToSolve = {ρgg, ρee, ρge, ρeg};
```

```
sol2 = DSolve[Eqns2, ToSolve, t];
```

```
Plot[Re[ρee[t] /. sol2] - Re[ρgg[t] /. sol2],
{t, 0, PulseDuration}, PlotRange → {-1, 1}]
```

